



BRUSH DC SERVO TECHNOLOGY

TERMS & DEFINITIONS

Servo motion systems excel in highly demanding industrial drive applications when rapid acceleration and precise positioning are critical to overall machine performance. Such systems are widely found in many industry applications including (but not limited to) machine tools, robotics, packaging, aerospace, textiles, woodworking, semiconductor fabrication, electronic assembly, medical applications, plastics & rubber, printing, labeling, food, drink & tobacco processing, material handling systems and factory automation.

DC Servo Systems

DC servo technology has existed as an excellent motion control solution in a vast number of industry applications for many decades. In spite of the widespread acceptance of brushless technology, DC systems continue to survive and flourish in the industrial marketplace. The success of brush DC systems can be attributed to a number of factors

- a) several decades of successful utilisation have resulted in a well tried and trusted solution
- b) DC systems are less complex than their brushless counterpart. In particular the drive is more readily understood and fewer wires allows for ease of system commissioning.
- c) The complete system is usually cheaper than its brushless counterpart especially when the motion demands are relatively simple.
- d) The DC system is a natural choice for battery driven motor.

The permanent magnet brush DC servo motor contains a rotating element with a wound armature terminated on a mechanical commutator. Power is transferred from the motor terminals to the commutator via carbon brushes. The commutator switches the direction of current in specific armature coils depending on the angular position of the armature. In this manner the brushes steer (commutate) the motor current into the armature so that optimum torque is produced. The permanent magnet field is set into the outer, non rotating stator (yoke). The stator completes the magnetic circuit and provides the mechanical support for the machine.

Electrical Parameters

The electrical parameters of a DC servomotor are usually presented in the form of a catalog data or electrical data sheet (see Fig. 1). These parameters often create considerable confusion. The terms and abbreviations used in the literature are described here, metric units being used throughout. Where relevant, the derivation of the terms is given, since this will assist in the application of the motors.

Terms and Definitions

Power (Rated) (Symbol – W, Units – Watts)

Normally the continuous power rating of the motor at maximum speed for a particular winding

$$\text{Power} = \text{Torque (Nm)} \times \text{Speed (rpm)} \times 2 \times \pi / 60 \quad \text{Watts}$$

Notes:-

- 1) The torque used in the above formulae is that which is permitted at the maximum speed of the motor. This is usually defined by the maximum allowable degree of brush sparking and/or brush life, except in the case of very low speed windings
- 2) The continuous Stall torque does not apply at maximum speed because of commutation limits and the reduction of available torque due to brush and bearing friction as speed increases

Max. Operating Speed (Symbol n_{max} , Units – rpm)

Normally the speed at which the terminal voltage is at its maximum permitted level. (In a few cases the maximum speed is governed by mechanical considerations instead of voltage)

Continuous Torque (Stall), (Symbol – Tc, Units – Nm)

The continuous torque rating of the motor at continuous current, ambient temperature of 40°C and speed approaching zero rpm. This figure is based on pure DC current and must be reduced by the Form Factor when using amplifiers other than unity Form Factor.

Continuous Torque $T_c = I_c \times K_t / F.F$ (Nm)

Where : I_c = Continuous Current
 K_t = Torque Constant
FF = Form Factor of Amplifier Used

The value of the rated torque is determined by the max permissible temperature of the armature winding which is in turn determined by the insulation class of the motor. Typically this is one of the following

Insul. Cl. A	105°C
Insul. Cl. E	120°C
Insul. Cl. B	130°C
Insul. Cl. F	155°C
Insul. Cl. H	180°C

Peak Torque (Symbol – Tp, Units – Nm)

The torque developed when the maximum permissible (peak) current is passed through the motor at standstill. Form Factor is not usually considered in this case, since peak current must not be passed through the motor for long periods.

Peak Torque $T_p = I_p \times K_t$ (Nm) **
where : I_p = Peak Current

** Note that this figure is usually reduced in practice by the effect of Armature Reaction, and so the value of T_p given in the motor specification should be used where it is less than the value calculated from the above equation. Note also that if the amplifier used has a peak output of less than the value of I_p for a given motor, then the motor's peak torque will be reduced pro rata.

Theoretical Acceleration (Symbol α_m , Units – rad/sec/sec)

This is the theoretical value of acceleration achieved away from standstill, when the motor is driven at peak current I_p , and so develops peak torque T_p . (with no load coupled to the motor)

Theoretical Acceleration $\alpha_m = T_p / J_m$ rad/sec/sec
Where : T_p = Peak Torque

$J_m = \text{Motor Inertia}$

Current at Continuous Torque (Symbol – I_c , Units – A)

The current needed to produce continuous torque. This is an average value. Since any current other than pure DC contains an AC component, the continuous current is normally derated by the Form Factor.

Current at Peak Torque (Symbol – I_p , Units – A)

The maximum current that can be passed through the motor at standstill. This may be limited by the brushes or the winding.

Maximum Terminal Voltage (Symbol – V_T , Units V)

The nominal maximum terminal voltage of the motor usually limited by the commutator.

$$\text{Terminal Voltage } V_T = (n/1,000) \times K_b + I_a \times R_m + V_b \text{ Volts}$$

Where : I_a = motor current at full speed

V_b = Brush voltage drop, usually assumed to be approx. 2 Volts

Note :- Where the motor does not have to run at its maximum terminal speed, the maximum terminal voltage will be reduced accordingly

Torque Sensitivity (Symbol – K_t , Units – Nm/A)

The relationship between the torque developed by the motor and the current flowing through it. This is a very important motor parameter. The effective value of K_t is reduced by the effect of armature reaction at high levels of current (see Peak Torque)

$$\text{Torque Constant} = (Z \times \phi \times p) / (2 \times n \times a) \quad \text{Nm/A}$$

where ϕ = flux/pole

p = number of poles

a = number of parallel paths
through the armature

Z = number of armature conductors

For a given motor design ϕ , P and a are fixed, but Z may be varied : increasing the number of turns increases Z and hence K_t . This gives rise to the different windings A, B, C etc. quoted for each size of motor.

At high levels of current K_t is reduced by the effect of armature reaction. This is the result of flux produced by the current in the armature windings partially opposing the flux produced by the field magnets.

Back E.M.F. Constant (Symbol – K_b , Units - V/krpm)

The voltage internally generated by the motor at 1,000 rpm.

$$\text{Back EMF Constant} = (1000 \times Z \times \phi \times p) / (60 \times a) \quad \text{V/krpm}$$

Note that from the equations for Back EMF constant and Torque Constant the important relationship

$$\mathbf{K_b (V/krpm) = 104.7 \times K_t (Nm/A)}$$

may be derived. Thus with a given motor design, it is not possible to change the K_b value without changing the K_t value by means of a winding change. Note also that K_b does not give the terminal voltage.

DC Resistance at 25°C (Symbol – R_m , Units - Ω)

The cold motor resistance, seen at its terminals, at room temperature. The temperature coefficient is typically 0.00388/°C

Inductance (Symbol - L_m , Units – mH)

The inductance of the motor, seen at its terminals

Mechanical Time Constant (Symbol - τ_m , Units - msec)

The response of the motor to a fixed voltage applied across the armature, ignoring friction, at 25°C.

This is the time for the motor to reach 63.2% of its final speed. The applied voltage must be such that the instantaneous current when the motor is at standstill does not exceed the peak current rating of the motor.

$$\text{Mech. Time Const. } \tau_m = J_m \times R_m \times 1,000 / K_t^2 \quad \text{msec}$$

where J_m = Motor Inertia

Electrical Time Constant (Symbol - τ_e , Units – msec)

The electrical time constant of the armature at 25°C

Elec. Time Const. $\tau_e = L_m / R_m$ msec
where L_m = Motor Inductance in mH
 R_m = Motor Resistance in Ohms

The following parameters relate to the tacho option

Voltage Sensitivity (Symbol – Kg, Units – V/krpm)

Tacho average output voltage per 1,000 rpm

Voltage Ripple (Symbol – Vr, Units - % pk-pk/avg.)

Tacho peak ripple expressed as a percentage of the average output.

The frequency of the ripple is also given in cycles per revolution (cy/rev).

		C.D.	91535-300	Issue	1	
		Written	P.O'Beirne	App'd.		
		Sheet	1	of	1	
DC Servomotor Tachometer		M4-2003-01A (TT2003)			02/01/2004	
Motor Parameters (DC)				Winding Data		
	Tol.	Symbol	Unit	A	C	D
Power	Rated	P	Watts	100	90	/
			hp	0.134	0.121	
Max. operating speed	Max	n max	rpm	6000	4500	4700
Continuous Torque (stall) @40°C ambient	Nom	Tc	Nm	0.45	0.45	0.34 *
			lb.ft	0.33	0.33	0.25
Peak Torque	Nom	Tp	Nm	2.15	2.35	0.85
			lb.ft	1.6	1.73	0.62
Theoretical Accl.	Nom	α m	rads/sec ²	23,900	26,100	9400
Current @ cont. torque	Rated	Ic	Amps	3.65	2.9	7 *
Current @ peak torque	Rated	Ip	Amps	18	15.3	18
Max. terminal voltage	Max	Vt	volts	90	90	24
Torque Sensitivity	+/- 10%	Kt	Nm/Amp	0.122	0.156	0.049
			lb.ft/Amp	0.09	0.115	0.036
Back EMF Constant	+/- 10%	Kb	V/Krpm	12.75	16.3	5.11
# DC Resistance @ 25°C	+/- 12.5%	Rm	Ohms	3.3	5.5	0.5
Inductance @ 1000Hz	+/- 30%	Lm	mH	3	4.7	0.45
Time Constant at 25°C	Mech	τ m	mSec	20	20	19
	Elec	τ e	mSec	0.91	0.85	0.93
# DOES NOT INCLUDE CONTACT DROP						
Tachometer Parameters (TGF 1568 A)				Winding Data		
				A		
Voltage Sensitivity	+/-10%	Kg	V/Krpm	7.0		
Volt ripple magnitude	Max %	Vr	pk-pk/avg	6		
Volt ripple frequency	Nom		cy/rev	26		
Elec. time constant	Nom		mSec			
DC Resistance	+/- 12.5%	Rg	Ω	43		
Load Resistance	Min	RL	Ω	10000		
Inductance	+/-30%	Lg	mH	25		
Basic Motor - Tachometer Constants						
Rotor Inertia	Jm	kg.m ²		0.00009	* Brush Limit Results	
		lb.ft.s ²		0.000066		
Weight	Wt	Kg (f)		2.2		
		lb		4.9		
Static Friction	Tf	Nm		0.03		
		lb.ft		0.022		
Thermal Time constant	TCT	minutes		20		
Viscous damping Z source	F1	Nm/krpm		0.005		
		lb.ft/krpm		0.004		

FIG. 1 Catalog Data Sheet for "M4-2006-01A" DC servomotor with integrated DC tachogenerator

